



**College of Arts and Sciences**  
**Department of Mathematics and Statistics**

**MTH 205 Course Syllabus –Summer 2009**

**Instructor Information**

Section	Professor	Room	Extension	E-mail
1&2	Ayman Badawi	NAB 262	2573	abadawi@aus.edu

**OFFICE HOURS**

Professor	Sun	Mon	Tue	Wed	Thu
Ayman Badawi	11:30-12:20	11:30-12:20	11:30-12:20	11:30-12:20	

**Course Information**

**Course number:** MTH 205

**Descriptive title:** Differential Equations

**Text:** *A First Course in Differential Equations with Modeling Applications*,  
 by D.G. Zill, 9<sup>th</sup> Edition.

**Objectives:** In this course we will be discussing the mathematical modeling of real-life problems, which usually leads to differential equations. We will also study different techniques of solving differential equations and boundary value problems. Students will be introduced to the concept of Laplace transforms and Transforms of derivatives, integrals and periodic functions. A greater emphasis will be on differential equations as mathematical models, nonlinear differential equations, and linear and nonlinear systems of differential equations.

Grading	%	Dates	Time
Test 1	22%	Sunday, June 28 (afternoon)	TBA
Test 2	44%	Sunday, July 12, (afternoon)	TBA
Test 3		Sunday, July 19, 2009 (afternoon)	TBA
Final Exam	34%	TBA	2 hours

**Remarks :**

**I will be AWAY from Tuesday June 16 – June 21. So No CLASS ON TUESDAY June 16. WE WILL MEET ON MONDAY JUNE 22.**

**MAKE UP CLASSES PLAN: TODAY, June 9. I will give a complete lecture and not just giving you hand outs (so we make up for one day). Three EXAMS WILL BE GIVEN OUTSIDE THE CLASS PERIOD and I will not dismiss the CLASSES for the DAY AFTER (so we make up for three classes).**

## **TABLE OF CONTENTS**

<b>1. Introduction to Differential Equations</b>	<b>1</b>
1.1 Definitions and Terminology	2
1.2 Initial-Value Problems	13
1.3 Differential Equations as Mathematical Models	19
<b>2. First-Order Differential Equations</b>	<b>34</b>
2.1 Solution Curves without a Solution	35
2.2 Separable Variables	44
2.3 Linear Equations	53
2.4 Exact Equations	62
2.5 Solutions by Substitutions	70
<b>3. Modeling with First-Order Differential Equations</b>	<b>82</b>
3.1 Linear Models	83
<b>4. Higher-Order Differential Equations</b>	<b>117</b>
4.1 Preliminary Theory - Linear Equations	118
4.2 Reduction of Order	130
4.3 Homogeneous Linear Equations with Constant Coefficients	133
4.4 Undetermined Coefficients – Superposition Approach	140
4.6 Variation of Parameters	157
4.7 Cauchy-Euler Equation	162
<b>5. Modeling with Higher-Order Differential Equations</b>	<b>181</b>
5.1 Linear Models: Initial-Value Problems	182
<b>7. The Laplace Transform</b>	<b>255</b>
7.1 Definition of the Laplace Transform	256
7.2 Inverse Transforms and Transforms of Derivatives	262
7.3 Operational Properties I	270
7.4 Operational Properties II	282
7.5 The Dirac Delta Function	292
7.6 Systems of Linear Differential Equations	295

## Math 205 - Suggested Problems

**TEXT:** *A First Course in Differential Equations, Ninth Edition.*  
*Dennis G. Zill*

**HOME WORK PROBLEMS FOR MTH 205:**

Use convolution to do PROBLEMS 31, 33, 32, 34 on Page 290 section 7.4.

Do 21, 25, 27, 29, 37, 41, 43, 45, 46 on section 7.4 page 290

---

For Periodic Functions: Page 290, 291 (7.4), Write down  $f(x)$ , find  $T$  then find  $L\{f(x)\}$  for number 49, 50, 51, 53, 5

For Delta, page 295 (7.5) do 1, 3, 7, 9

For system of equations Page 299 (after Thursday Lecture) (7.6) Do 1, 3, 7, 11

---

For section 4.3 Page 138 I recommend : 1, 5, 9, 13, 15, 17, 25, 29, 41.

I STRONGLY RECOMMEND YOU LOOK AT EXAMPLE 2 on page 142

I recommend that you look at PAGE 144 (TABLE 4.1 FOR Particular Solution  $y_p$ )

-----

For section 4.4 Page 148 I recommend: 1, 5, 11, 13, 15, 21, 26, 29, 31, 36, 37, 39, 41

---

For 4.6 (Variation) THE BOOK HAS EXCELLENT PROBLEMS: YOU MUST DO 1, 5, 9, 11, 13, 19, 21 on page 161-162.

---

Section 2.3 (Linear Diff. Equation) Page 60: 5, 7, 17, 19 (GOOD ONE), 21, 22 (so good), 24 (really good), 29, 30, 34 (ok but boring)

---

Page 194 (Spring, 5.1): 3, 5, 9, 11, 23, 29, 31 (I will discuss amplitude, Frequency, and period Later on...Do not worry about that in Question number 11)

Page 198 (Circuit, 5.1): 45, 49, 53

Page 89 (Growth, Decay, 3.1): 3, 5, 6, 7

---

***HW on Bernoulli section 2.5***

Page 74 section 2.5: Problems: 15, 17, 20, 21

---

Separable (Section 2.2 page 50): 3, 7, 11, 21, 23, 25, 29, 31 (THESE ARE GOOD PROBLEMS, MUST DO)

Exact ( Section 2.4, Page 68): 3, 4, 7, 13(Can you do it using Linear D.E?), , 16, 23

Reduced to separable (Section 2.5, Page 74): 11, 12 (This is a nice Problem, first FIND  $dy/dx$ , then you can use Bernoulli..NICE) , , 23, 24, 25, 29.

---

Cauchy (Section 4.7, page 168): 1, 5, 13, 19, 23, 27, 29

Reduced second order (Section 4.2, page 132) 15 and 16

Autonomous Page 43 section 2.1. Just do 21, 23, 24, 25 AS WE DID in the class

